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**Research Paper** 



# Prediction of the Maximum Surface Settlement Induced by Urban Area Tunneling Using Multiple Linear Regression Model and Random Forest Algorithm

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Abstract: The occurrence of settlement induced by tunneling operations in urban environments is an inevitable phenomenon. The risk of damage to nearby infrastructures and surface structures can be greatly reduced by predicting and controlling this event. This paper uses multiple linear regression (MLR) model and random forest (RF) algorithm to predict the maximum surface settlement (Smax) due to shallow tunnel excavation. Nine input parameters, including the distance of the tunnel center from the ground surface (H), height of the underground water level above the tunnel (W.T), tunnel diameter (D), elastic modulus of soil (E), undrained shear strength of soil (Cu), earth pressure coefficient  $(K_0)$ , unit weight of soil ( $\gamma$ ), gap parameter (g), and stability number (N) were selected from 24 data sets related to 14 tunneling projects. The MLR and RF techniques were then implemented for predicting Smax. Three performance indicators of coefficient of determination (R<sup>2</sup>), root mean square error (RMSE), and mean absolute error (MAE) were employed for the training and test phases to evaluate the efficiency of the suggested models. The coefficient of determination values for MLR and RF for training data were 0.814 and 0.957, respectively, while for test data were 0.793 and 0.96, indicating that the RF approach is more efficient than MLR. Moreover, the findings reveal that the RF algorithm exhibits lower RMSE and MAE values in both the training and testing phases compared to the MLR method. This suggests that the RF algorithm exhibits reduced error and higher reliability and accuracy when compared to the MLR model. Also, the performance study demonstrates that among the input parameters, the gap parameter (g) and the undrained shear strength of soil (Cu) have the greatest and least influence on Smax, respectively.

*Keywords:* Tunneling operations, Maximum surface settlement (Smax), Multiple linear regression (MLR) model, Random forest (RF) algorithm.

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### **INTRODUCTION**

Ground settlement resulting from tunnelling operations is an inevitable occurrence that poses a significant concern in urban underground projects. The ability to predict and control this phenomenon is essential to reduce possible damage to surface structures and nearby infrastructures. Due to the importance of the settlement and its direct impact on the project costs, so far many studies have been conducted based on different methods as well as presenting relationships to predict it. Various methods, including empirical, analytical, numerical, and artificial intelligence approaches are available. In practice, ground movement prediction is mainly based on empirical relationships that do not consider the intrinsic parameters of the soil [1-4]. Although analytical methods are useful tools for predicting  $S_{max}$  and present a closed-form solution, they cannot include all the parameters affecting the settlement [5-8]. In numerical methods, mathematical equations are solved using the finite element [9] or discrete element [10] method to predict the movement of the overburden layers and, finally, the settlement of the ground surface is calculated.

In contrast to the three aforesaid methods, artificial intelligence methods provide the possibility of analysing a larger amount of data by integrating complex nonlinear combinations to predict the target parameter. In this paper, using the two methods of multiple linear regression (MLR) model and random forest (RF) algorithm, the amount of  $S_{max}$  resulting from tunneling operations is predicted. The results showed that RF algorithm can predict  $S_{max}$  more accurately than MLR model.

#### **METHODS**

In this study, multiple linear regression (MLR) model and random forest (RF) algorithm were used to predict  $S_{max}$  induced by tunneling operations. MLR is a statistical methodology that is widely employed to estimate the result of a variable predicted by the value of two or more variables. Random Forest (RF) is a type of ensemble learning technique, originally introduced by Breiman in 2001 [11], designed to enhance the accuracy of classification and regression tree (CART) models by integrating a vast collection of decision trees. Decision trees can be classified into two categories, namely, classification and regression trees [11]. Given that the primary goal of this research is to predict  $S_{max}$  caused by tunneling operations, we only focus on the regression mode. The RF regression technique is classified as a nonparametric regression methodology.

#### FINDINGS AND ARGUMENT

In order to attain the optimal version of MLR and RF models for predicting  $S_{max}$ , their performances are assessed throughout the training and testing phases by utilizing three performance indicators: determination coefficient (R<sup>2</sup>), root mean square error (RMSE), and mean absolute error (MAE). Through the utilization of the trial and error methodology, the optimal MLR and RF models are achieved. The values of the aforesaid indicators for the training and test phase data are shown in Table 1. Figure 1 displays the acquired relationship between the measured and predicted values of  $S_{max}$  from both the RF and MLR models within the training and testing stages. As illustrated in Figure 1, the MLR and RF models exhibit R<sup>2</sup> values of 0.814 and 0.957, respectively, when predicting  $S_{max}$  during the training phase. In the testing phase, these models yield R<sup>2</sup> values of 0.793 and 0.96, respectively. Moreover, the findings reveal that the RF algorithm exhibits lower RMSE and MAE values in both the training and testing phases compared to the MLR method. This suggests that the RF algorithm exhibits reduced error and higher reliability and accuracy when compared to the MLR model. From the results obtained above, it can be inferred that the RF algorithm demonstrates greater reliability and heightened accuracy when compared to the MLR model in its ability to predict  $S_{max}$  induced by tunneling operations. Furthermore, the RF results reveal a strong correlation with the measured

index	Train phase		Test phase	
	RF	MLR	RF	MLR
R <sup>2</sup>	0.9569	0.8139	0.9605	0.7934
RMSE	9.36	15.93	9.94	38.42
MAE	6.84	12.64	8.38	29.09

Table 1. Values of statistical indicators in training and testing phases of MLR and RF models



Figure 1. The relationship of measured and predicted values of the  $S_{max}$  in training and testing phases of RF and MLR models

data and align closely with the actual values. Consequently, it can be deduced that the RF algorithm serves as a suitable tool for the prediction of  $S_{max}$  resulting from tunneling operations conducted in urban environments.

Based on the methodology employed to assess importance, the impact values of 9 input variables on the resulting  $S_{max}$  value derived from the RF algorithm are computed and presented in Figure 2. It is evident that the parameter g holds the highest importance in determining  $S_{max}$ . Conversely, the parameter  $C_u$  is of the least importance in modeling the  $S_{max}$  parameter.

## CONCLUSIONS

In this paper, using two methods of multiple linear regression (MLR) and random forest (RF) algorithm, the prediction of  $S_{max}$  caused by tunneling operations in urban environments was studied. MLR and RF methods were implemented based on 24 data sets related to different tunneling projects and selection of 9 variables as influencing parameters on  $S_{max}$ . In the first stage, 80% of the data were used as training data and 20% as test data to implement the suggested methods. Then, in order to evaluate the efficiency of the used methods, three performance indicators of the coefficient of determination parameter (R<sup>2</sup>), root mean square error (RMSE), and mean absolute error (MAE) were used for the training and test data. The results of the models showed that the R<sup>2</sup> values of MLR and RF methods for training data are 0.814 and 0.957, respectively, and for test data are 0.793 and 0.96, respectively. Also, the findings demonstrate that the RF algorithm exhibits lower RMSE and MAE values in both the training and testing phases compared to the



Figure 2. The result of importance study for  $S_{max}$  modeling

MLR method. The obtained results indicate the higher efficiency and accuracy of RF method compared to MLR. Finally, variable importance (VI) index was utilized to determine the most and least important parameters affecting  $S_{max}$ . The obtained results showed that among the input parameters, the gap parameter (g) and the undrained shear strength of soil ( $C_{u}$ ) have the greatest and least influence on  $S_{max}$ , respectively.

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